

Kinetic Theory with Algebra

Suppose that the box contains N molecules (N in the whole box, not N molecules in each cubic meter as in some texts). Suppose that the box has length a meters and ends of dimensions b meters by c meters.

In the course of their random motion with many collision the molecules will exchange momentum, p , and will not all keep the same velocity. However, if the temperature is kept constant, we believe their velocities will range around a fixed average velocity, which we call v meters/sec. To calculate the pressure on one end of the box we deal only with molecular impacts on that end. So to simplify the problem we pretend that the N molecules are regimented in three equal groups, one lot moving up-and-down, one lot to-and-fro across the width, and one lot moving forwards-and-backwards along the length. For the pressure on one end we then consider the last lot only. Symmetry-considerations suggest we should imagine the molecules equally divided among the three groups. Making these assumptions, answer the questions below, using m kilograms for the mass of one molecule.

- (i) When one molecule hits the front end head-on and rebounds, its change of momentum is
- (ii) Between successive impacts on the *front end* a molecule travels to the other end and back: a total distance _____ meters.
- (iii) In a total time t seconds, a molecule moving with velocity v meters/sec travels a total distance
- (iv) \therefore in t seconds, a molecule can make _____ round trips and so can make this number of impacts on the front end.
- (v) \therefore in t seconds, a molecule makes _____ impacts on the front end of box, suffering at each impact a change of momentum _____
- (vi) \therefore total change in momentum, due to impacts of *one* molecule, suffered by front end in t seconds is
- (vii) But there are N molecules in the box, of which _____ are in the group moving forward and backward between the ends.
 \therefore the total change of momentum, due to impacts of all molecules concerned, suffered by the front end in t seconds is _____

- (viii) But, $Ft = \Delta p$ $\therefore F = \Delta p/t$
 and in this case the average *Force*, during their period of t seconds,
 on the front end of the box is¹
- (ix) $P = F/A$, and the area of the end face is
 \therefore average *Pressure* on the end of the box is
- (x) The volume of the box is m³.
 \therefore the product $PV =$
 But m is the mass of one molecule, and there are N molecules,
 so the *total mass of gas* in the box M kg = kg.
 Substituting M into the algebra above, we have
 $PV =$
- (xi) Providing we use a closed box or other apparatus allowing no leakage
 of gas, then M is constant. Suppose we keep temperature constant;
 then other experiments in physics suggest that the average velocity
 v remains constant. Then in this case when the volume is changed
 the result of (x) above suggests that
- (xii) If we measure the *volume* of a sample of gas, say in a globe, and
 find its mass (by weighing the globe full of gas and then evacuated),
 and measure the *pressure* of the sample with a barometer, then
 the result of (x) above enables us to calculate a very important
 piece of information, the value of, which is the
 of the molecules.
- (xiii) UNITS TO BE USED. In making the calculation of (xii) above if
 the volume is in m³ the mass should be in
 and the pressure should be in
- (xiv) We have already derived two useful things from our molecular theory,
 a behavior-suggestion in (xi) and a very interesting measurement
 in (xii), and more results will emerge; but we must pay for them
 by the assumptions that go into the machine. *List on a separate
 sheet as many assumptions as you can*, (a) of general physical
 laws assumed to apply to molecules, (b) of special properties,
 of behavior, size, etc., assumed for molecules.

¹Here, t is the time during which the average force would have to act to
 produce this momentum-change. Therefore t IS the time t seconds for which we
 have calculated the total momentum-change.